

SULIT

NO. KAD PENGENALAN

ANGKA GILIRAN

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**LEMBAGA PEPERIKSAAN
KEMENTERIAN PELAJARAN MALAYSIA**

SIJIL PELAJARAN MALAYSIA 2012

3472/1

ADDITIONAL MATHEMATICS

Kertas 1

Nov./Dis.

2 jam

Dua jam

JANGAN BUKA KERTAS SOALANINI SEHINGGA DIBERITAHU

1. Tulis nombor kad pengenalan dan angka giliran anda pada petak yang disediakan.
 2. Kertas soalan ini adalah dalam dwibahasa.
 3. Soalan dalam bahasa Inggeris mendahului soalan yang sepadan dalam bahasa Melayu.
 4. Calon dibenarkan menjawab keseluruhan atau sebahagian soalan sama ada dalam bahasa Inggeris atau bahasa Melayu.
 5. Calon dikehendaki membaca maklumat di halaman belakang kertas soalan ini.

Untuk Kegunaan Pemeriksa			
Kod Pemeriksa:	Soalan	Markah Penuh	Markah Diperoleh
	1	2	
	2	4	
	3	3	
	4	3	
	5	3	
	6	3	
	7	3	
	8	3	
	9	3	
	10	4	
	11	3	
	12	4	
	13	4	
	14	2	
	15	2	
	16	3	
	17	3	
	18	4	
	19	4	
	20	3	
	21	3	
	22	3	
	23	4	
	24	4	
	25	3	
	Jumlah	80	

Kertas soalan ini mengandungi 23 halaman bercetak dan 1 halaman tidak bercetak.

[Lihat halaman sebelah
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The following formulae may be helpful in answering the questions. The symbols given are the ones commonly used.

Rumus-rumus berikut boleh membantu anda menjawab soalan. Simbol-simbol yang diberi adalah yang biasa digunakan.

ALGEBRA

$$1 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$8 \quad \log_a b = \frac{\log_c b}{\log_c a}$$

$$2 \quad a^m \times a^n = a^{m+n}$$

$$9 \quad T_n = a + (n-1)d$$

$$3 \quad a^m \div a^n = a^{m-n}$$

$$10 \quad S_n = \frac{n}{2}[2a + (n-1)d]$$

$$4 \quad (a^m)^n = a^{mn}$$

$$11 \quad T_n = ar^{n-1}$$

$$5 \quad \log_a mn = \log_a m + \log_a n$$

$$12 \quad S_n = \frac{a(r^n - 1)}{r-1} = \frac{a(1 - r^n)}{1-r}, \quad r \neq 1$$

$$6 \quad \log_a \frac{m}{n} = \log_a m - \log_a n$$

$$7 \quad \log_a m^n = n \log_a m$$

$$13 \quad S_\infty = \frac{a}{1-r}, \quad |r| < 1$$

CALCULUS KALKULUS

$$1 \quad y = uv, \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

4 Area under a curve
Luas di bawah lengkung

$$= \int_a^b y \, dx \text{ or (atau)}$$

$$2 \quad y = \frac{u}{v}, \quad \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

$$= \int_a^b x \, dy$$

$$3 \quad \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

5 Volume of revolution
Isi padu kisaran

$$= \int_a^b \pi y^2 \, dx \text{ or (atau)}$$

$$= \int_a^b \pi x^2 \, dy$$

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**STATISTICS
STATISTIK**

1
$$\bar{x} = \frac{\sum x}{N}$$

7
$$\bar{I} = \frac{\sum W_i I_i}{\sum W_i}$$

2
$$\bar{x} = \frac{\sum f x}{\sum f}$$

8
$${}^n P_r = \frac{n!}{(n-r)!}$$

3
$$\sigma = \sqrt{\frac{\sum (x - \bar{x})^2}{N}} = \sqrt{\frac{\sum x^2}{N} - \bar{x}^2}$$

9
$${}^n C_r = \frac{n!}{(n-r)! r!}$$

4
$$\sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}} = \sqrt{\frac{\sum f x^2}{\sum f} - \bar{x}^2}$$

10
$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

5
$$m = L + \left(\frac{\frac{1}{2}N - F}{f_m} \right) C$$

11
$$P(X = r) = {}^n C_r p^r q^{n-r}, p + q = 1$$

12 Mean / Min , $\mu = np$

13
$$\sigma = \sqrt{npq}$$

14
$$Z = \frac{X - \mu}{\sigma}$$

6
$$I = \frac{Q_1}{Q_0} \times 100$$

**GEOMETRY
GEOMETRI**

1 Distance / Jarak

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

5
$$|\underline{r}| = \sqrt{x^2 + y^2}$$

2 Midpoint / Titik tengah

$$(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

6
$$\hat{\mathbf{r}} = \frac{x\underline{\mathbf{i}} + y\underline{\mathbf{j}}}{\sqrt{x^2 + y^2}}$$

 3 A point dividing a segment of a line
Titik yang membahagi suatu tembereng garis

$$(x, y) = \left(\frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n} \right)$$

4 Area of triangle / Luas segi tiga

$$= \frac{1}{2} |(x_1 y_2 + x_2 y_3 + x_3 y_1) - (x_2 y_1 + x_3 y_2 + x_1 y_3)|$$

TRIGONOMETRY
TRIGONOMETRI

1 Arc length, $s = r\theta$
Panjang lengkok, s = j\theta

2 Area of sector, $A = \frac{1}{2}r^2\theta$
Luas sektor, L = \frac{1}{2}j^2\theta

3 $\sin^2 A + \cos^2 A = 1$
 $\sin^2 A + \cos^2 A = 1$

4 $\sec^2 A = 1 + \tan^2 A$
 $\sec^2 A = 1 + \tan^2 A$

5 $\operatorname{cosec}^2 A = 1 + \cot^2 A$
 $\operatorname{cosec}^2 A = 1 + \cot^2 A$

6 $\sin 2A = 2 \sin A \cos A$
 $\sin 2A = 2 \sin A \cos A$

7 $\cos 2A = \cos^2 A - \sin^2 A$
 $= 2 \cos^2 A - 1$
 $= 1 - 2 \sin^2 A$

$\cos 2A = \cos^2 A - \sin^2 A$
 $= 2 \cos^2 A - 1$
 $= 1 - 2 \sin^2 A$

8 $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
 $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$

9 $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
 $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$

10 $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$

11 $\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$

12 $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

13 $a^2 = b^2 + c^2 - 2bc \cos A$
 $a^2 = b^2 + c^2 - 2bc \cos A$

14 Area of triangle / *Luas segi tiga*

$$= \frac{1}{2}ab \sin C$$

Answer all questions.
Jawab semua soalan.

- 1 Diagram 1 shows the relation between set M and set N .
Rajah 1 menunjukkan hubungan antara set M dan set N .

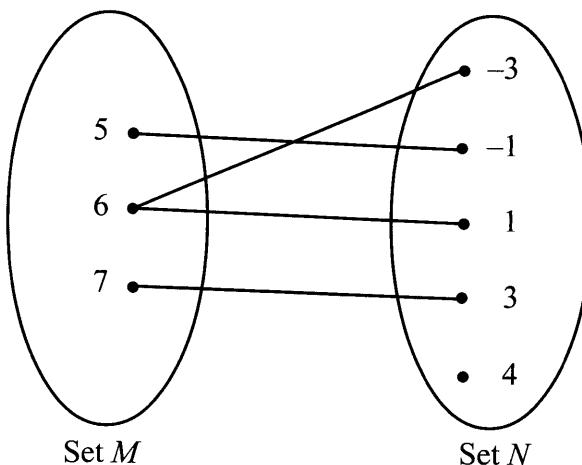


Diagram 1
Rajah 1

State

Nyatakan

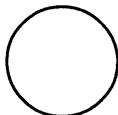
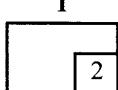
- (a) the object of -1 ,
objek bagi -1 ,
- (b) the range of the relation.
julat hubungan itu.

[2 marks]
[2 markah]

Answer / Jawapan:

(a)

(b)



- 2** Given that $f(x) = 3x + 4$ and $fg(x) = 6x + 7$, find
Diberi $f(x) = 3x + 4$ dan $fg(x) = 6x + 7$, cari

(a) $fg(4)$,

(b) $g(x)$.

[4 marks]
[4 markah]

Answer / Jawapan:

(a)

(b)

2

4

- 3** Given that $f: x \rightarrow x + 5$, find

Diberi $f: x \rightarrow x + 5$, cari

(a) $f(3)$,

(b) the value of k such that $2f^{-1}(k) = f(3)$.

nilai k dengan keadaan $2f^{-1}(k) = f(3)$.

[3 marks]
[3 markah]

Answer / Jawapan:

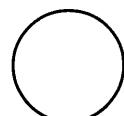
(a)

(b)

3

3

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SULIT

8

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- 4 It is given that 3 and $m + 4$ are the roots of the quadratic equation $x^2 + (n - 1)x + 6 = 0$, where m and n are constants.

Find the value of m and of n .

Diberi bahawa 3 dan $m + 4$ ialah punca-punca bagi persamaan kuadratik $x^2 + (n - 1)x + 6 = 0$, dengan keadaan m dan n ialah pemalar.

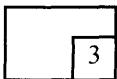
Cari nilai m dan nilai n .

[3 marks]

[3 markah]

Answer / Jawapan:

4



- 5 A quadratic equation $x(x - 4) = h - 2k$, where h and k are constants, has two equal roots.

Express h in terms of k .

Persamaan kuadratik $x(x - 4) = h - 2k$, dengan keadaan h dan k ialah pemalar, mempunyai dua punca sama.

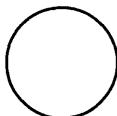
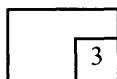
Ungkapkan h dalam sebutan k .

[3 marks]

[3 markah]

Answer / Jawapan:

5



- 6 Given that $f(x) = -3x^2 + 2x + 13$, find the range of values of x for $f(x) \leq 5$. [3 marks]
Diberi $f(x) = -3x^2 + 2x + 13$, *cari julat nilai* x *untuk* $f(x) \leq 5$. [3 markah]

Answer / Jawapan:

6
3

- 7 Solve the equation:

Selesaikan persamaan:

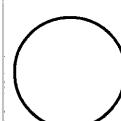
$$27(3^{2x+4}) = 1$$

[3 marks]
[3 markah]

Answer / Jawapan:

7
3

[Lihat halaman sebelah
SULIT]



SULIT

10

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- 8** Solve the equation:

Selesaikan persamaan:

$$1 + \log_2(x - 2) = \log_2 x$$

[3 marks]

[3 markah]

Answer / Jawapan:

8

3

- 9** The first three positive terms of a geometric progression are 2, p and 18.

Find the value of p and the common ratio of the progression.

Tiga sebutan pertama yang positif bagi suatu janjang geometri ialah 2, p dan 18.

Cari nilai p dan nisbah sepunya bagi janjang itu.

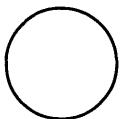
[3 marks]

[3 markah]

Answer / Jawapan:

9

3



- 10** It is given that 11 , $y + 4$ and $3y - x$ are three consecutive terms of an arithmetic progression.

Diberi bahawa 11 , $y + 4$ *dan* $3y - x$ *ialah tiga sebutan berturutan bagi suatu janjang aritmetik.*

- (a) Express y in terms of x .

Ungkapkan y *dalam sebutan* x .

- (b) Find the common difference if $x = 8$.

Cari beza sepunya jika $x = 8$.

[4 marks]

[4 markah]

Answer / Jawapan:

(a)

(b)

10

4

- 11** In a geometric progression, the first term is a and the common ratio is r .

Given that the third term of the progression exceeds the second term by $12a$, find the values of r .

Dalam suatu janjang geometri, sebutan pertama adalah a *dan nisbah sepunya ialah* r .

Diberi sebutan ketiga janjang itu melebihi sebutan kedua sebanyak $12a$, *cari nilai-nilai* r .

[3 marks]

[3 markah]

Answer / Jawapan:

11

3

Lihat halaman sebelah
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- 12 The variables x and y are related by the equation $\frac{p}{y} = 1 - \frac{q}{x^2}$. Diagram 12 shows the straight line graph obtained by plotting $\frac{1}{y}$ against $\frac{1}{x^2}$.

Pembolehubah x dan y dihubungkan oleh persamaan $\frac{p}{y} = 1 - \frac{q}{x^2}$. Rajah 12

menunjukkan graf garis lurus yang diperoleh dengan memplot $\frac{1}{y}$ melawan $\frac{1}{x^2}$.

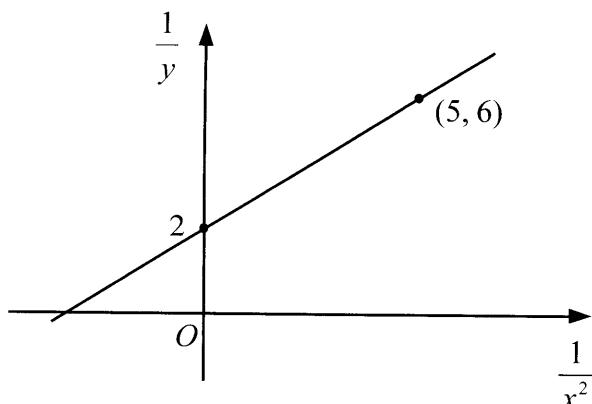


Diagram 12

Rajah 12

Find the value of

Cari nilai

(a) p ,

(b) q .

[4 marks]

[4 markah]

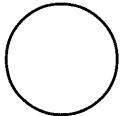
Answer / Jawapan:

(a)

(b)

12

4



13 Diagram 13 shows a straight line AB .

Rajah 13 menunjukkan suatu garis lurus AB .

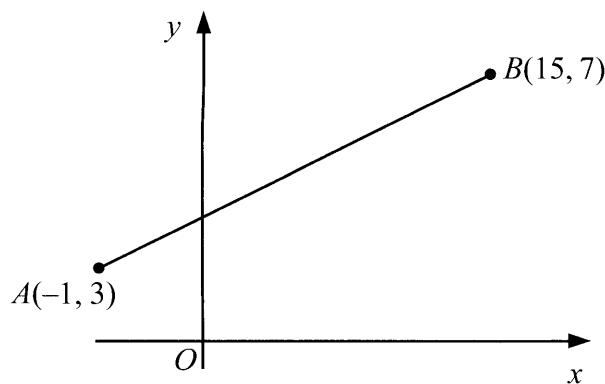


Diagram 13
Rajah 13

Find

Cari

(a) the midpoint of AB ,

titik tengah AB ,

(b) the equation of the perpendicular bisector of AB .

persamaan pembahagi dua sama serenjang AB .

[4 marks]
[4 markah]

Answer / Jawapan:

(a)

(b)

13

4

Lihat halaman sebelah
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- 14 Diagram 14 shows a straight line PQ with the equation $\frac{x}{10} + \frac{y}{2k} = 1$.

Rajah 14 menunjukkan satu garis lurus PQ yang mempunyai persamaan $\frac{x}{10} + \frac{y}{2k} = 1$.

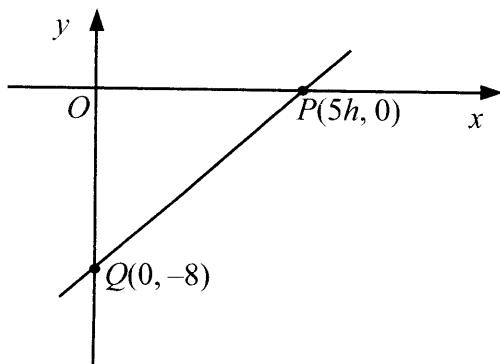


Diagram 14
Rajah 14

Determine the value of

Tentukan nilai

(a) h ,

(b) k .

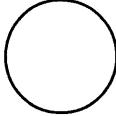
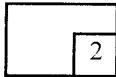
[2 marks]
[2 markah]

Answer / Jawapan:

(a)

(b)

14



- 15** Diagram 15 shows the vectors \overrightarrow{OA} , \overrightarrow{OB} and \overrightarrow{OP} drawn on a grid of equal squares with sides of 1 unit.

Rajah 15 menunjukkan vektor \overrightarrow{OA} , \overrightarrow{OB} dan \overrightarrow{OP} dilukis pada grid segi empat sama yang sama besar bersisi 1 unit.

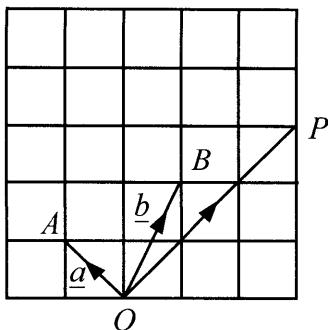


Diagram 15
Rajah 15

Determine

Tentukan

- (a) $|\overrightarrow{OP}|$,
 (b) \overrightarrow{OP} in terms of \underline{a} and \underline{b} .
 \overrightarrow{OP} dalam sebutan \underline{a} dan \underline{b} .

[2 marks]
[2 markah]

Answer / Jawapan:

(a)

(b)

15

	2
--	---

[Lihat halaman sebelah
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SULIT

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- 16** The following information refers to the vectors \underline{a} and \underline{b} .

Maklumat berikut adalah berkaitan dengan vektor \underline{a} dan \underline{b} .

$$\underline{a} = \begin{pmatrix} 6 \\ m-4 \end{pmatrix}, \quad \underline{b} = \begin{pmatrix} 2 \\ 5 \end{pmatrix}$$

It is given that $\underline{a} = k\underline{b}$, where \underline{a} is parallel to \underline{b} and k is a constant.

Diberi bahawa $\underline{a} = k\underline{b}$, dengan keadaan \underline{a} selari dengan \underline{b} dan k ialah pemalar.

Find the value of

Cari nilai

- (a) k ,
(b) m .

[3 marks]

[3 markah]

Answer / Jawapan:

(a)

(b)

16

3

- 17** Solve the equation $\tan^2 \theta - 3 \tan \theta + 2 = 0$ for $0 \leq \theta \leq 360^\circ$.

[3 marks]

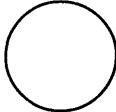
Selesaikan persamaan $\tan^2 \theta - 3 \tan \theta + 2 = 0$ untuk $0 \leq \theta \leq 360^\circ$.

[3 markah]

Answer / Jawapan:

17

3



18 Diagram 18 shows sectors OAB and ODC with centre O .

Rajah 18 menunjukkan sektor OAB dan sektor ODC dengan pusat O .

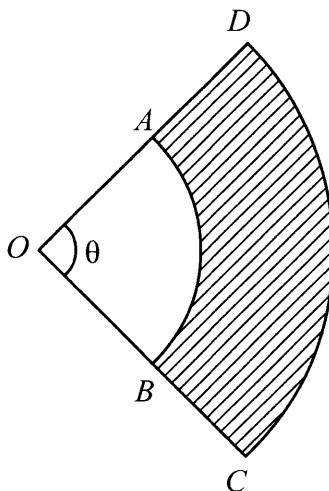


Diagram 18
Rajah 18

It is given that $OA = 4 \text{ cm}$, the ratio of $OA : OD = 2 : 3$ and the area of the shaded region is 11.25 cm^2 .

Find

Diberi bahawa $OA = 4 \text{ cm}$, nisbah $OA : OD = 2 : 3$ dan luas kawasan berlorek ialah 11.25 cm^2 .

Cari

- (a) the length, in cm, of OD ,
panjang, dalam cm, OD ,
- (b) θ , in radians.
 θ , *dalam radian.*

[4 marks]
[4 markah]

Answer / Jawapan:

(a)

(b)

18

4

[Lihat halaman sebelah
SULIT]

- 19 Given the function $h(x) = kx^3 - 4x^2 + 5x$, find

Diberi fungsi $h(x) = kx^3 - 4x^2 + 5x$, cari

(a) $h'(x)$,

(b) the value of k if $h''(1) = 4$.

nilai k jika $h''(1) = 4$.

[4 marks]
[4 markah]

Answer / Jawapan:

(a)

(b)

19

4

- 20 The gradient of the tangent to the curve $y = x^2(2 + px)$ at $x = -2$ is 7.

Find the value of p .

Kecerunan tangen kepada lengkung $y = x^2(2 + px)$ di $x = -2$ ialah 7.

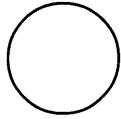
Cari nilai p .

[3 marks]
[3 markah]

Answer / Jawapan:

20

3



21 Given that $\int_2^7 f(x)dx = 10$, find

Diberi bahawa $\int_2^7 f(x)dx = 10$, cari

(a) the value of $\int_7^2 f(x)dx$,

nilai $\int_7^2 f(x)dx$,

(b) the value of k if $\int_2^7 [f(x)-k]dx = 25$.

nilai k jika $\int_2^7 [f(x)-k]dx = 25$.

[3 marks]
[3 markah]

Answer / Jawapan:

(a)

(b)

21

3

Lihat halaman sebelah
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- 22 The mass of a group of 6 students has a mean of 40 kg and a standard deviation of 3 kg.

Jisim satu kumpulan 6 orang pelajar mempunyai min 40 kg dan sisihan piawai 3 kg.

Find

Cari

- (a) the sum of the mass of the students,
hasil tambah jisim pelajar-pelajar itu,
- (b) the sum of the squares of the mass of the students.
hasil tambah kuasa dua jisim pelajar-pelajar itu.

[3 marks]

[3 markah]

Answer / Jawapan:

(a)

(b)

22

3

-
- 23 There are 10 different coloured marbles in the box.

Dalam sebuah kotak terdapat 10 biji guli yang berlainan warna.

Find

Cari

- (a) the number of ways 3 marbles can be chosen from the box,
bilangan cara 3 biji guli boleh dipilih dari kotak itu,
- (b) the number of ways at least 8 marbles can be chosen from the box.
bilangan cara sekurang-kurangnya 8 biji guli boleh dipilih dari kotak itu.

[4 marks]

[4 markah]

Answer / Jawapan:

(a)

(b)

23

4

- 24 A box contains 20 chocolates. 5 of the chocolates are black chocolates flavour and the other 15 are white chocolates flavour. Two chocolates are taken at random from the box.

Find the probability that

Sebuah kotak mengandungi 20 biji coklat. 5 daripadanya adalah perisa coklat hitam manakala 15 lagi itu adalah perisa coklat putih. Dua biji coklat diambil secara rawak dari kotak itu.

Cari kebarangkalian bahawa

- (a) both chocolates are black chocolates,

kedua-dua biji coklat adalah coklat hitam,

- (b) the chocolates taken are of different flavour.

coklat yang diambil mempunyai perisa yang berlainan.

[4 marks]

[4 markah]

Answer / Jawapan:

(a)

(b)

24

4

[Lihat halaman sebelah
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- 25** In a test, 60% of the students has passed. A sample of 8 students is chosen at random.

Find the probability that more than 6 students from the sample passed the test.

Dalam suatu ujian, 60% daripada pelajar telah lulus. Satu sampel yang terdiri daripada 8 pelajar dipilih secara rawak.

Cari kebarangkalian bahawa lebih daripada 6 pelajar daripada sampel itu lulus ujian tersebut.

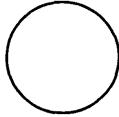
[3 marks]

[3 markah]

Answer / Jawapan:

25

3



**END OF QUESTION PAPER
KERTAS SOALAN TAMAT**

INFORMATION FOR CANDIDATES
MAKLUMAT UNTUK CALON

1. This question paper consists of **25** questions.
*Kertas soalan ini mengandungi **25** soalan.*
2. Answer **all** questions.
*Jawab **semua** soalan.*
3. Write your answers in the spaces provided in the question paper.
Tulis jawapan anda dalam ruang yang disediakan dalam kertas soalan.
4. Show your working. It may help you to get marks.
Tunjukkan langkah-langkah penting dalam kerja mengira anda. Ini boleh membantu anda untuk mendapatkan markah.
5. If you wish to change your answer, cross out the answer that you have done. Then write down the new answer.
Sekiranya anda hendak menukar jawapan, batalkan jawapan yang telah dibuat. Kemudian tulis jawapan yang baru.
6. The diagrams in the questions provided are not drawn to scale unless stated.
Rajah yang mengiringi soalan tidak dilukis mengikut skala kecuali dinyatakan.
7. The marks allocated for each question are shown in brackets.
Markah yang diperuntukkan bagi setiap soalan ditunjukkan dalam kurungan.
8. A list of formulae is provided on pages 3 to 5.
Satu senarai rumus disediakan di halaman 3 hingga 5.
9. A booklet of four-figure mathematical tables is provided.
Sebuah buku sifir matematik empat angka disediakan.
10. You may use a scientific calculator.
Anda dibenarkan menggunakan kalkulator saintifik.
11. Hand in this question paper to the invigilator at the end of the examination.
Serahkan kertas soalan ini kepada pengawas peperiksaan di akhir peperiksaan.